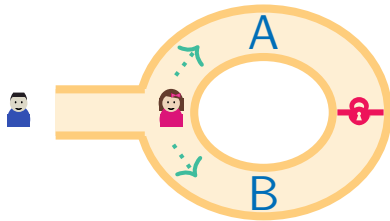


Sudoku

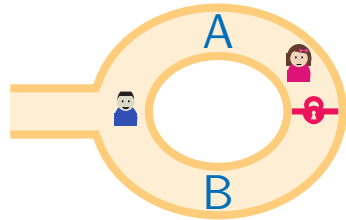
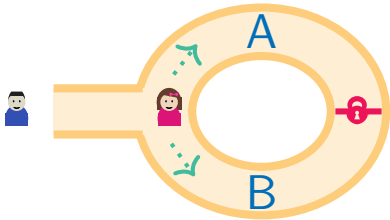
	2		5	1		9	
8			2	3			6
	3			6		7	
		1			6		
5	4					1	9
		2			7		
	9			3		8	
2			8	4			7
	1		9	7		6	

Unsolved Sudoku

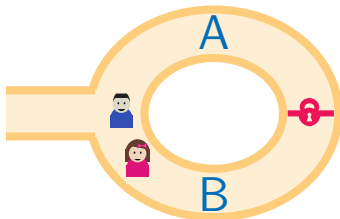
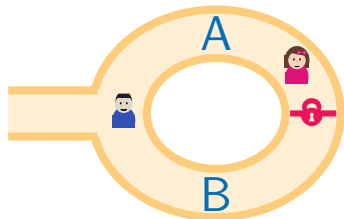
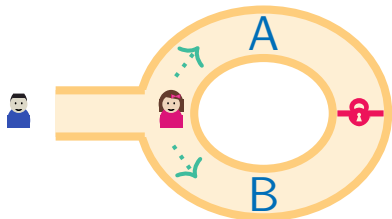
Ali-Baba cave



Ali-Baba cave



Ali-Baba cave



A need for new primitives

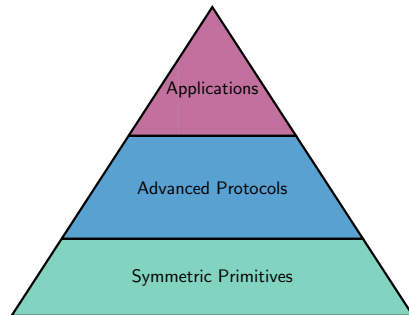
Protocols requiring new primitives:

★ **FHE**: Fully Homomorphic Encryption

★ **MPC**: Multiparty Computation

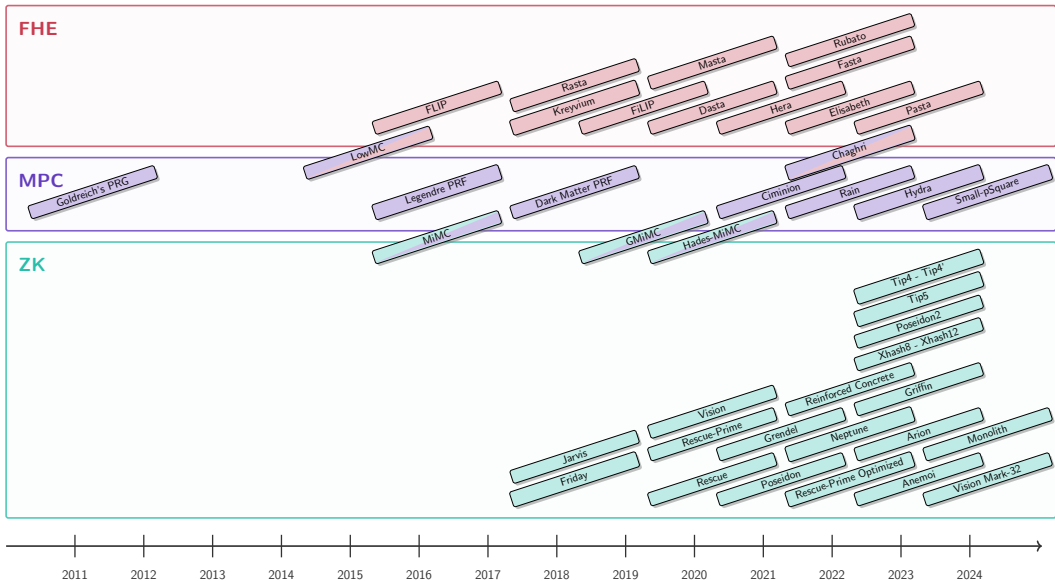
★ **ZK**: Systems of Zero-Knowledge proofs

Example: SNARKs, STARKs, Bulletproofs



Problem: Designing new symmetric primitives

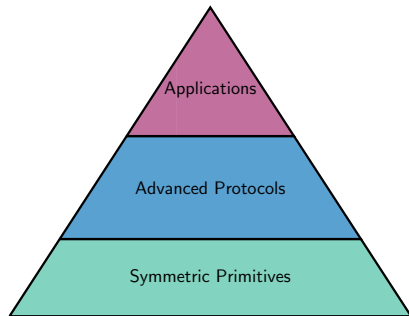
Primitives



A need for new primitives

Protocols requiring new primitives:

- ★ **FHE**: Fully Homomorphic Encryption
- ★ **MPC**: Multiparty Computation
- ★ **ZK**: Systems of Zero-Knowledge proofs
Example: SNARKs, STARKs, Bulletproofs



Problem: Designing new symmetric primitives

And analyse their security!

Content

- ★ Symmetric cryptography and cryptanalysis tools

- ★ Introduction of **AOP**



- ★ Attacks against **AOP**



Block ciphers

- ★ input: n -bit block

$$x \in \mathbb{F}_2^n$$

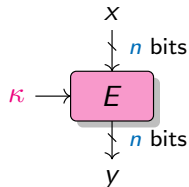
- ★ parameter: k -bit key

$$\kappa \in \mathbb{F}_2^k$$

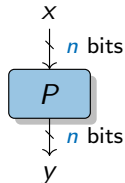
- ★ output: n -bit block

$$y = E_{\kappa}(x) \in \mathbb{F}_2^n$$

- ★ symmetry: E and E^{-1} use the same κ



(a) Block cipher



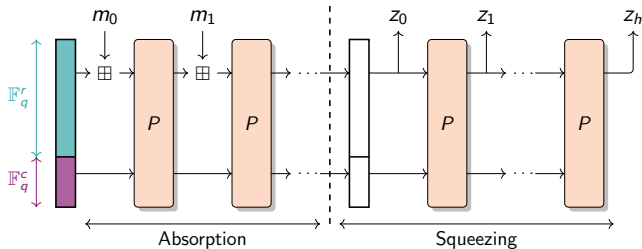
(b) Random permutation

Sponge construction

Sponge construction

Parameters:

- ★ rate $r > 0$
- ★ capacity $c > 0$
- ★ permutation of \mathbb{F}_q^n ($n = r + c$)

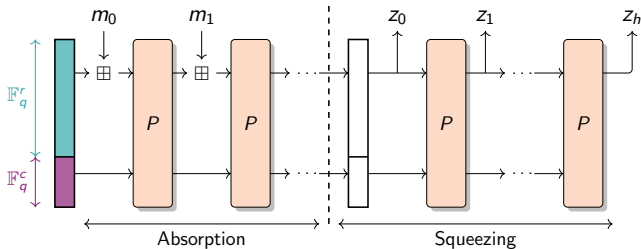


Sponge construction

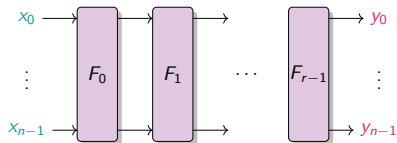
Sponge construction

Parameters:

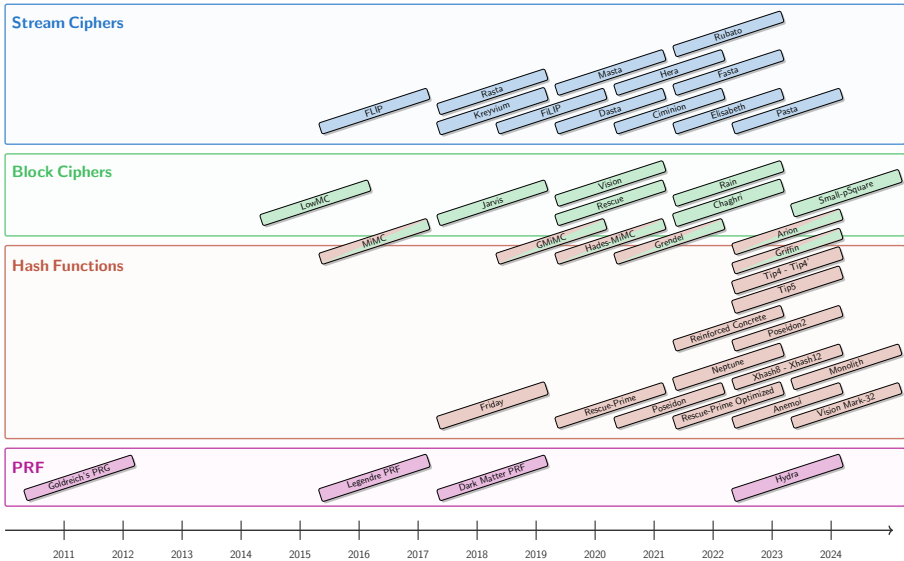
- ★ rate $r > 0$
- ★ capacity $c > 0$
- ★ permutation of \mathbb{F}_q^n ($n = r + c$)



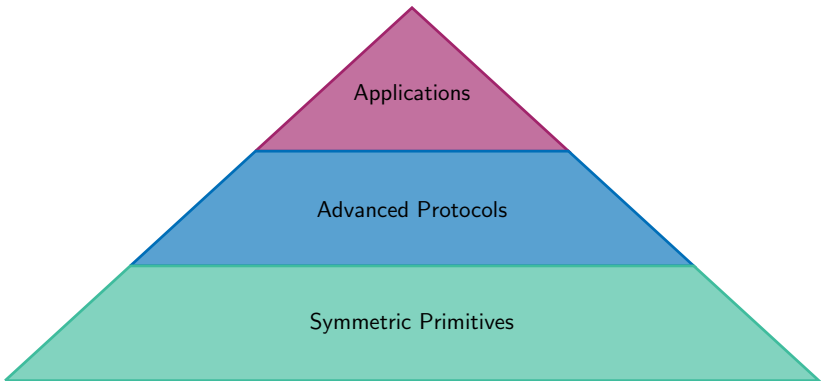
P is an iterated construction



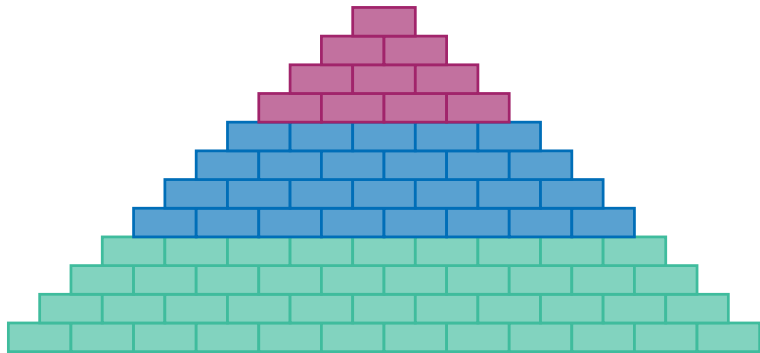
Primitives



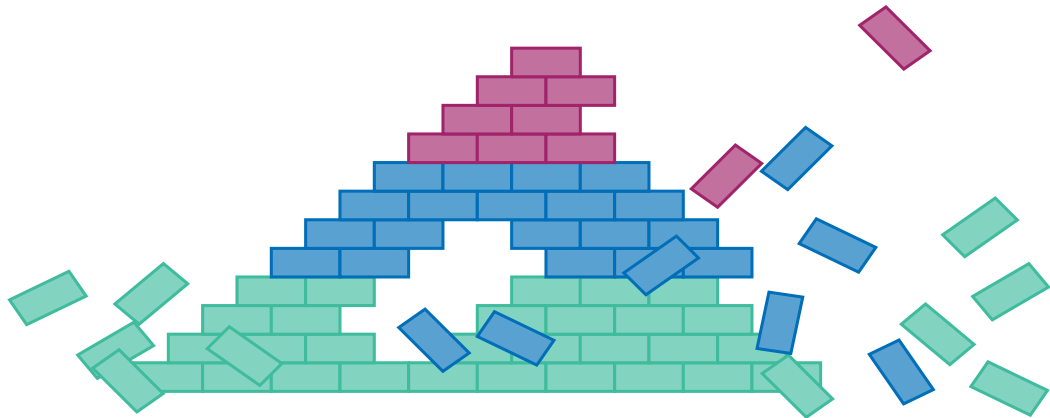
Building blocks of security



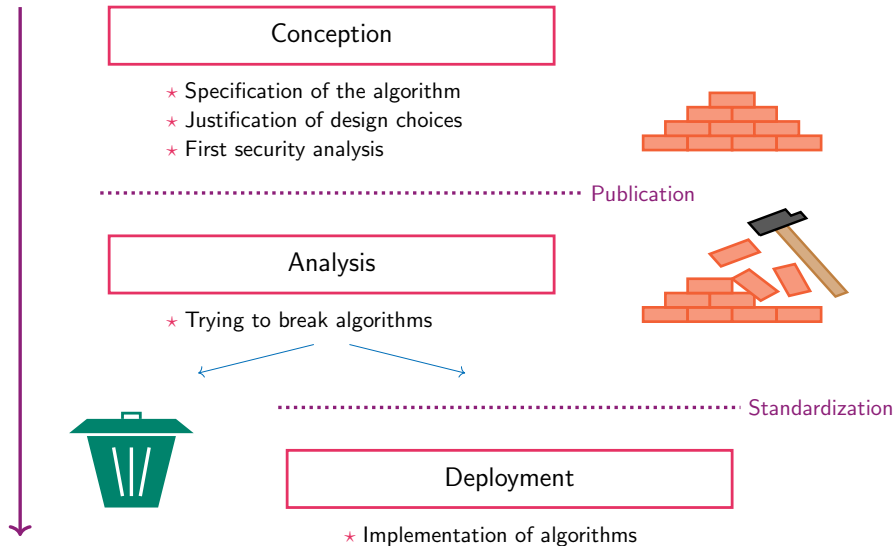
Building blocks of security



Cycle primitive



Primitive life cycle



CICO problem

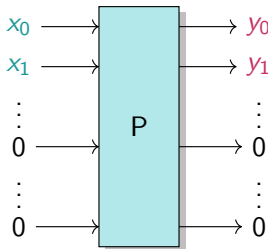
CICO: Constrained Input Constrained Output

Definition

Let $P : \mathbb{F}_q^{r+c} \rightarrow \mathbb{F}_q^{r+c}$. The **CICO** problem is:

Finding $X, Y \in \mathbb{F}_q^r$ s.t.

$$P(X, 0^c) = (Y, 0^c)$$



Content

Introduction of AOP



A new environment

Traditional case

Operations based on logical gates or CPU instructions.

$$\mathbb{F}_2^n, \text{ with } n \simeq 4, 8$$

Example

Field of AES

$$\mathbb{F}_2^n, \text{ where } n = 8$$

$$(0, 0, 0, 0, 0, 0, 0, 0),$$

$$(0, 0, 0, 0, 0, 0, 0, 1),$$

...

$$(1, 1, 1, 1, 1, 1, 1, 1)$$

A new environment

Traditional case

Operations based on **logical gates** or **CPU instructions**.

$$\mathbb{F}_2^n, \text{ with } n \simeq 4, 8$$

Example

Field of **AES**

$$\mathbb{F}_2^n, \text{ where } n = 8$$

(0, 0, 0, 0, 0, 0, 0, 0),

(0, 0, 0, 0, 0, 0, 0, 1),

...

(1, 1, 1, 1, 1, 1, 1, 1)

Arithmetization-Oriented

Operations based on **large finite-field arithmetic**.

$$\mathbb{F}_q, \text{ with } q \in \{2^n, p\}, p \simeq 2^n, n \geq 32$$

Example

Scalar Field of Curve **BLS12-381**

$$\mathbb{F}_p, \text{ where}$$

$p = 0x73eda753299d7d483339d80809a1d805$

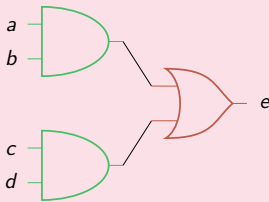
$53bda402fffe5bfeffffffff00000001$

$0, 1, 2, \dots, p - 1$

New operations

Traditional case

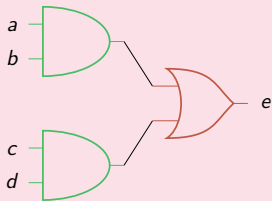
Use of **logical gates** and **CPU instructions**.



New operations

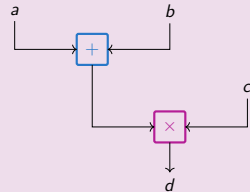
Traditional case

Use of **logical gates and CPU instructions.**



Arithmetization-Oriented

Use of **Arithmetic circuit.**

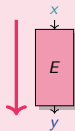


A new metric

Traditional case

Minimize time and memory.

$$y \leftarrow E(x)$$

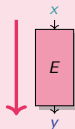


A new metric

Traditional case

Minimize **time and memory**.

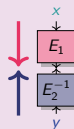
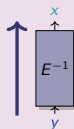
$$y \leftarrow E(x)$$



Arithmetization-Oriented

Minimize the number of **multiplications**.

$$y \leftarrow E(x) \quad \text{and} \quad y == E(x)$$

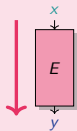


A new metric

Traditional case

Minimize **time and memory**.

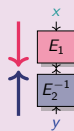
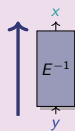
$$y \leftarrow E(x)$$



Arithmetization-Oriented

Minimize the number of **multiplications**.

$$y \leftarrow E(x) \quad \text{and} \quad y == E(x)$$



Example

Let $E : \mathbb{F}_{11} \rightarrow \mathbb{F}_{11}, x \mapsto x^3$. We have $E^{-1} : \mathbb{F}_{11} \rightarrow \mathbb{F}_{11}, x \mapsto x^7$.

Evaluation: Given $x = 5$, compute $y = E(x)$.

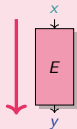
$$y = 4 \text{ (applying } E)$$

A new metric

Traditional case

Minimize **time and memory**.

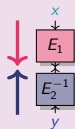
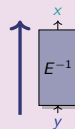
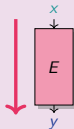
$$y \leftarrow E(x)$$



Arithmetization-Oriented

Minimize the number of **multiplications**.

$$y \leftarrow E(x) \quad \text{and} \quad y == E(x)$$



Example

Let $E : \mathbb{F}_{11} \rightarrow \mathbb{F}_{11}, x \mapsto x^3$. We have $E^{-1} : \mathbb{F}_{11} \rightarrow \mathbb{F}_{11}, x \mapsto x^7$.

Verification: Given $x = 5$ and $y = 4$, check if $y = E(x)$.

$$5^3 = 4 \quad (\text{applying } E) \quad \text{or} \quad 4^7 = 5 \quad (\text{applying } E^{-1})$$

Take-away

Traditional case

- ★ Alphabet:

$$\mathbb{F}_2^n, \text{ with } n \simeq 4, 8$$

- ★ Operations:
Logical gates/CPU instructions
- ★ Metric: minimize time and memory for the **evaluation**
- ★ **Decades of Cryptanalysis**

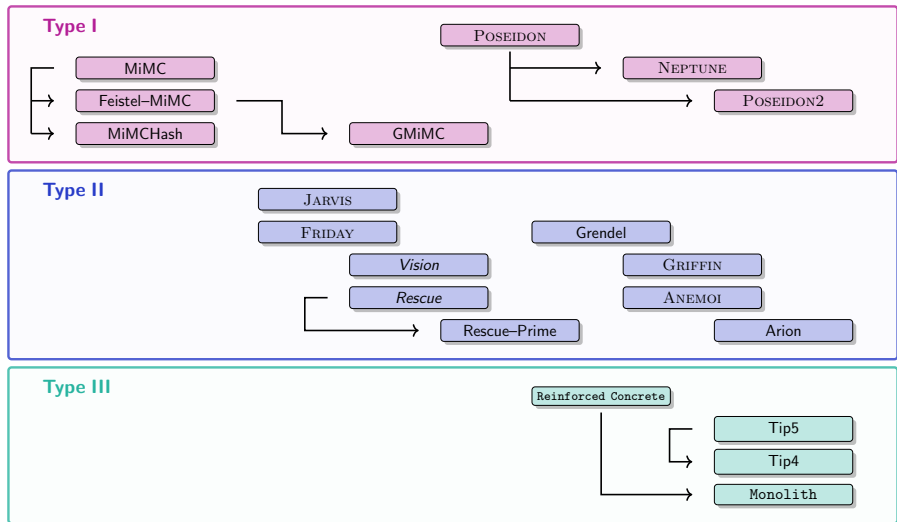
Arithmetization-Oriented

- ★ Alphabet:

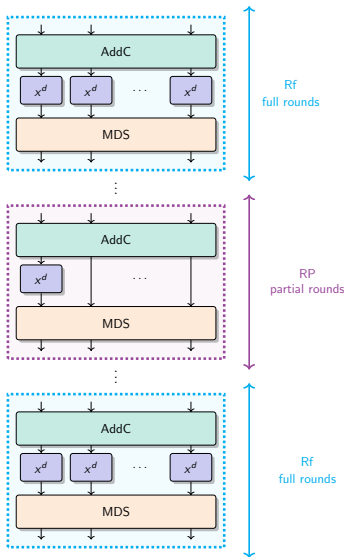
$$\mathbb{F}_q, \text{ with } q \in \{2^n, p\}, p \simeq 2^n, n \geq 32$$

- ★ Operations:
Large finite-field arithmetic
- ★ Metric: minimize the number of multi-
plications for the **verification**
- ★ ≤ 8 **years of Cryptanalysis**

Primitives overview



Example of Type I: POSEIDON



Low degree primitive

L. Grassi, D. Khovratovich, C. Rechberger, A. Roy and M. Schafneger, 2021

★ S-box:

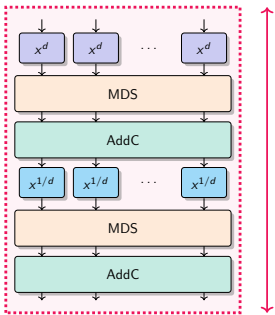
$$x \mapsto x^3$$

★ Nb rounds:

$$R = 2 \times Rf + RP$$

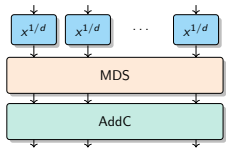
$$= 8 + (\text{from } 56 \text{ to } 84)$$

Example of Type II: *Rescue*



1 round
(2 steps)

⋮



Primitive based on equivalence

A. Aly, T. Ashur, E. Ben-Sasson, S. Dhooghe and A. Szepieniec, 2020

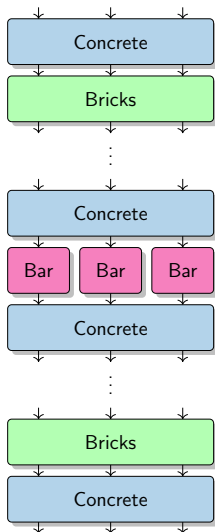
★ S-box:

$$x \mapsto x^3 \quad \text{and} \quad x \mapsto x^{1/3}$$

★ Nb rounds:

$R =$ from 8 to 26
(2 S-boxes per round)

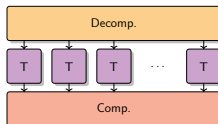
Example of Type III: Reinforced Concrete



Primitive using Look-up-Tables

L. Grassi, D. Khovratovich, R. Lüftenegger, C. Rechberger, M. Schofneger and R. Walch, 2022

★ S-box:



★ Nb rounds:

$$R = 7$$

Take-away

	Type I	Type II	Type III
	Low-degree primitives	Equivalence relation	Look-up tables
Alphabet	\mathbb{F}_q^m for various q and m	\mathbb{F}_q^m for various q and m	specific fields
Nb of rounds	many	few	fewer
Plain performance	fast	slow	faster
Nb of constraints	often more	fewer	it depends on the proof system

QUIZ !!

To which type of primitives (I, II, or III) belong AES?



QUIZ !!

Could we use AES for advanced protocols?



Content

Attacks against AOP



CICO Problem

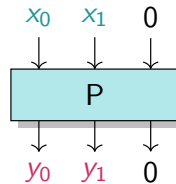
CICO: Constrained Input Constrained Output

Definition

Let $P : \mathbb{F}_q^t \rightarrow \mathbb{F}_q^t$ and $u < t$.

The **CICO** problem is:

Finding $X, Y \in \mathbb{F}_q^{t-u}$ s.t. $P(X, 0^u) = (Y, 0^u)$.



when $t = 3$, $u = 1$.

Need to solve polynomial systems

Solving polynomial systems

★ **Univariate** solving: find the roots of $\mathcal{P}_j \in \mathbb{F}_q[X]$

$$\begin{cases} \mathcal{P}_0(X) & = 0 \\ & \vdots \\ \mathcal{P}_{m-1}(X) & = 0 . \end{cases}$$

Solving polynomial systems

★ **Univariate** solving: find the roots of $\mathcal{P}_j \in \mathbb{F}_q[X]$

$$\begin{cases} \mathcal{P}_0(X) & = 0 \\ & \vdots \\ \mathcal{P}_{m-1}(X) & = 0 . \end{cases}$$

★ **Multivariate** solving: find the roots of $\mathcal{P}_j \in \mathbb{F}_q[X_0, \dots, X_{n-1}]$

$$\begin{cases} \mathcal{P}_0(X_0, \dots, X_{n-1}) & = 0 \\ & \vdots \\ \mathcal{P}_{m-1}(X_0, \dots, X_{n-1}) & = 0 . \end{cases}$$

Euclidean division

★ Integers

$$a = q \times b + r, 0 \leq r < b$$

Example: division of 2025 by 100

$$2025 = 20 \times 100 + 25$$

Euclidean division

★ Integers

$$a = q \times b + r, 0 \leq r < b$$

Example: division of 2025 by 100

$$2025 = 20 \times 100 + 25$$

★ Univariate polynomials

$$A = Q \times B + R, 0 \leq \deg(R) < \deg(B)$$

Example: division of $X^5 + 2X^3 + 3X$ by X^2

$$X^5 + 2X^3 + 3X = (X^3 + 2X) \times X^2 + 3X$$

Euclidean division

★ Integers

$$a = q \times b + r, \quad 0 \leq r < b$$

Example: division of 2025 by 100

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★ Multivariate polynomials

Euclidean division

★ Integers

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Example: division of 2025 by 100

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★ Univariate polynomials

$$A = Q \times B + R, \quad 0 \leq \deg(R) < \deg(B)$$

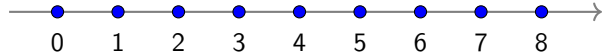
Example: division of $X^5 + 2X^3 + 3X$ by X^2

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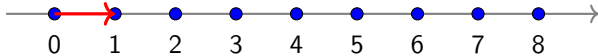
★ Multivariate polynomials

Need monomial ordering

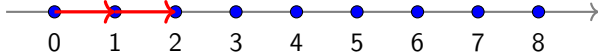
Monomial ordering



Monomial ordering



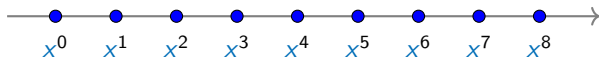
Monomial ordering



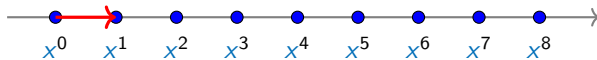
Monomial ordering



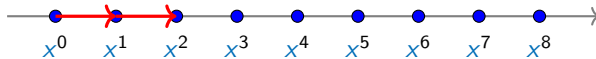
Monomial ordering



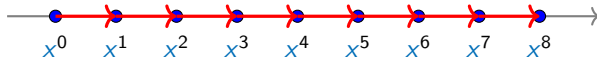
Monomial ordering



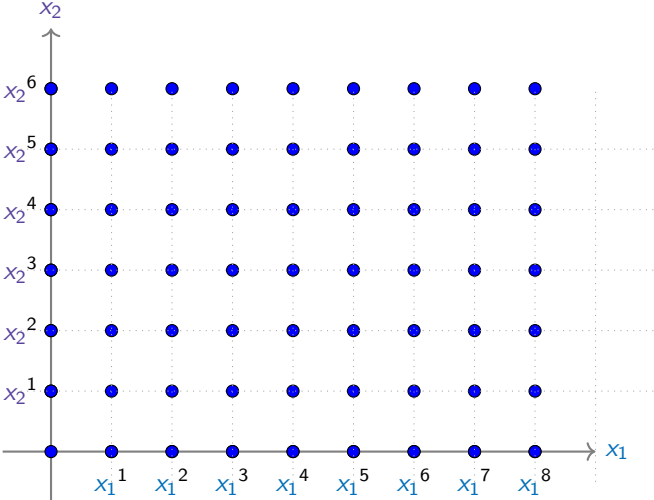
Monomial ordering



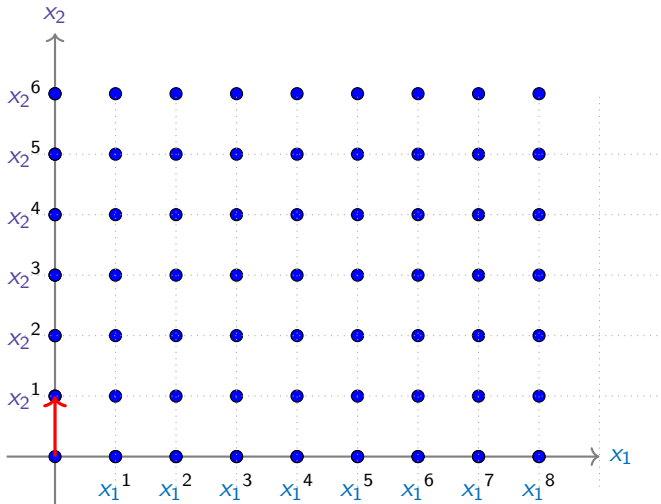
Monomial ordering



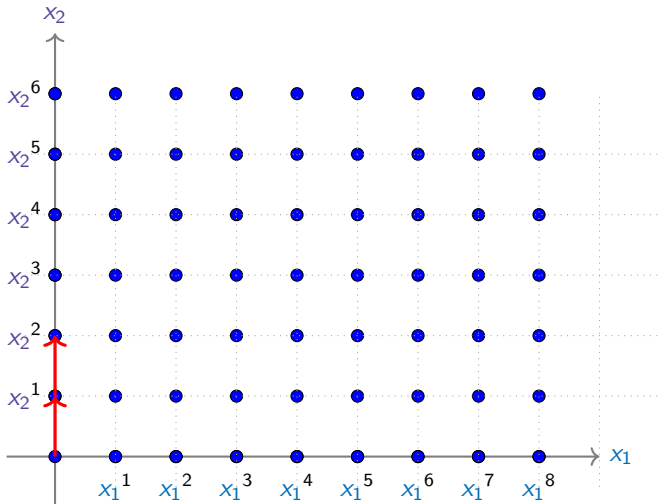
Lexicographical ordering



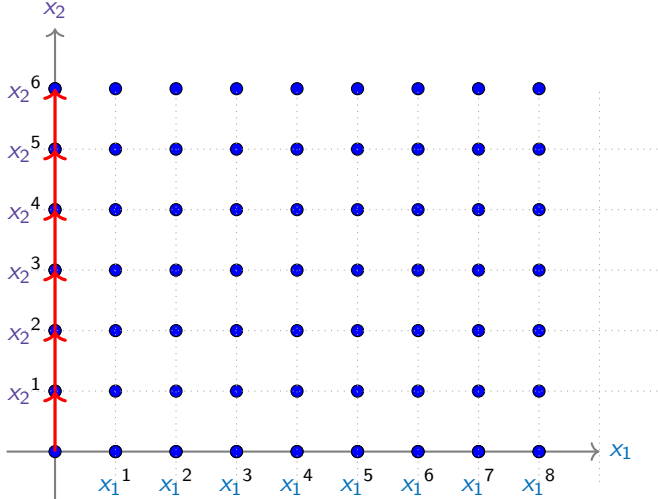
Lexicographical ordering



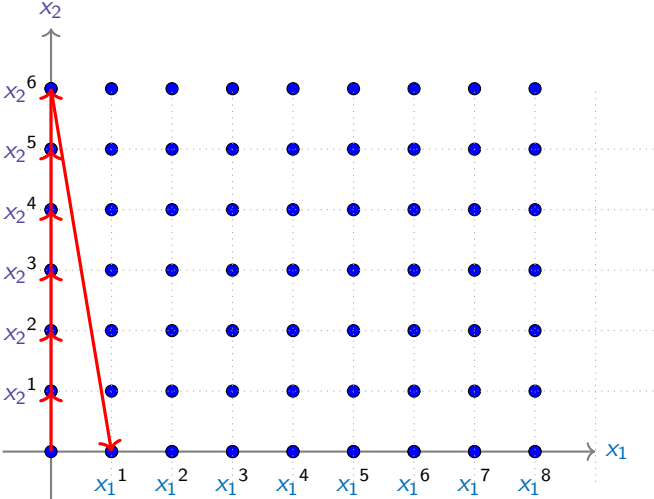
Lexicographical ordering



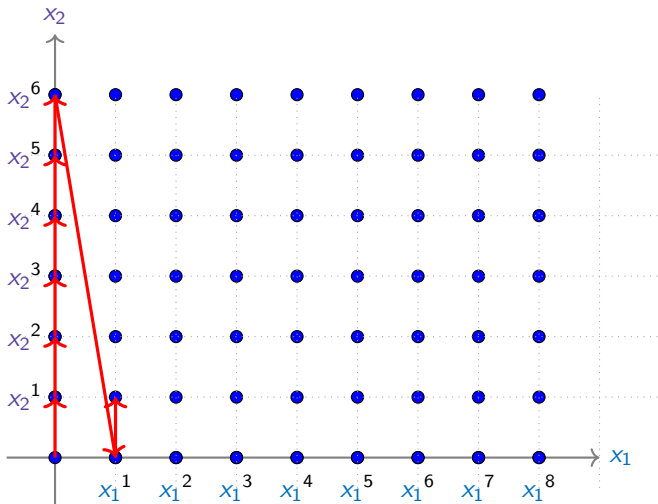
Lexicographical ordering



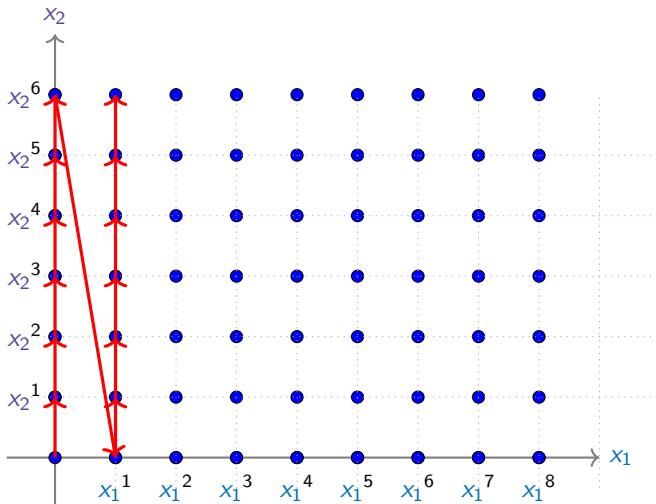
Lexicographical ordering



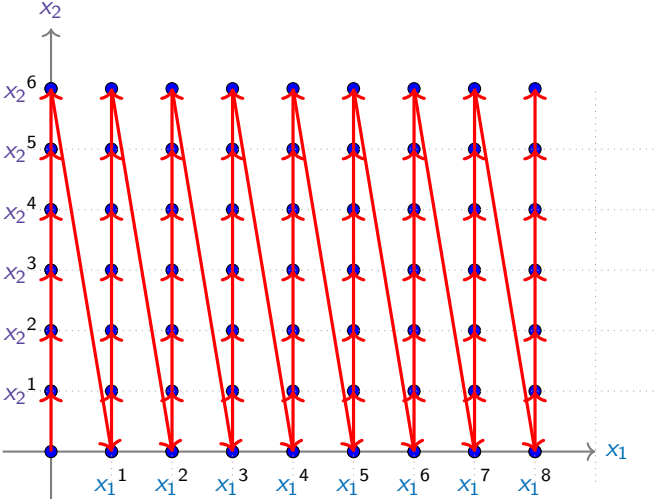
Lexicographical ordering



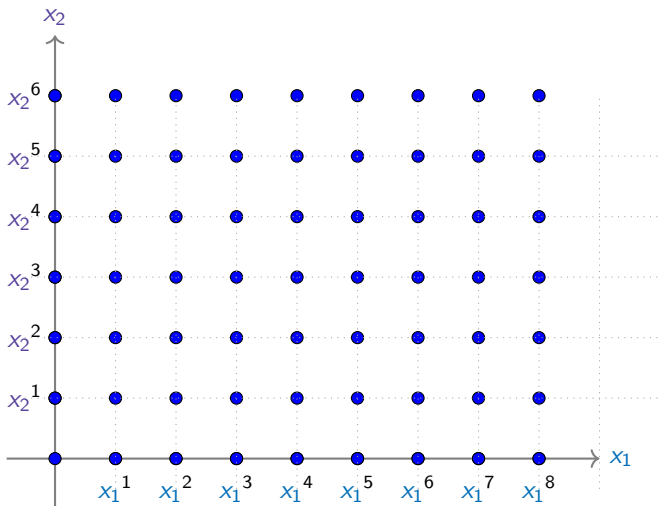
Lexicographical ordering



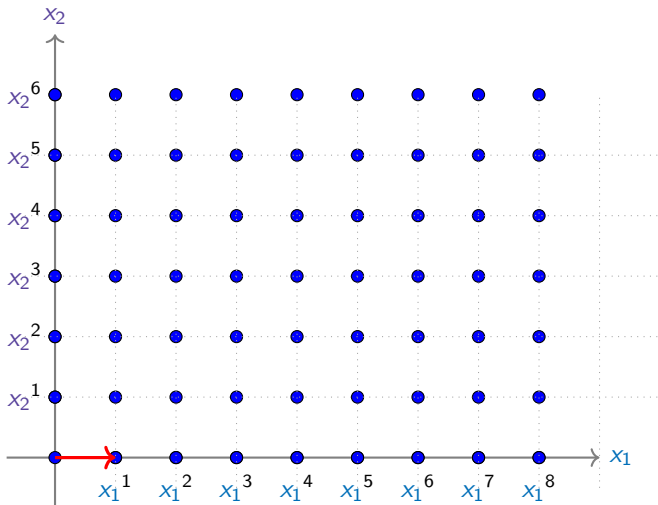
Lexicographical ordering



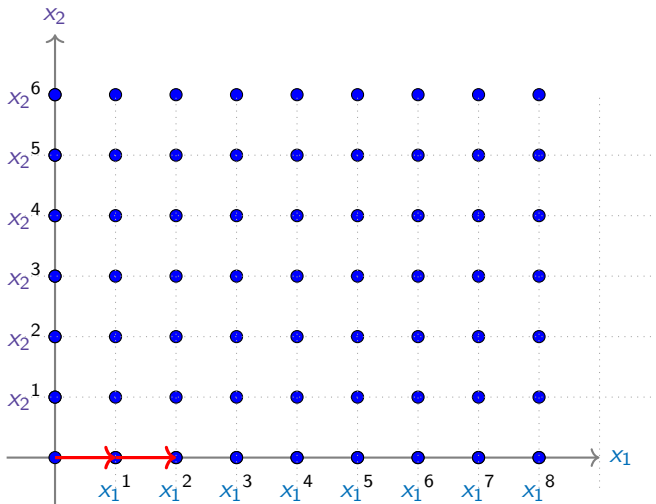
Reverse lex. ordering



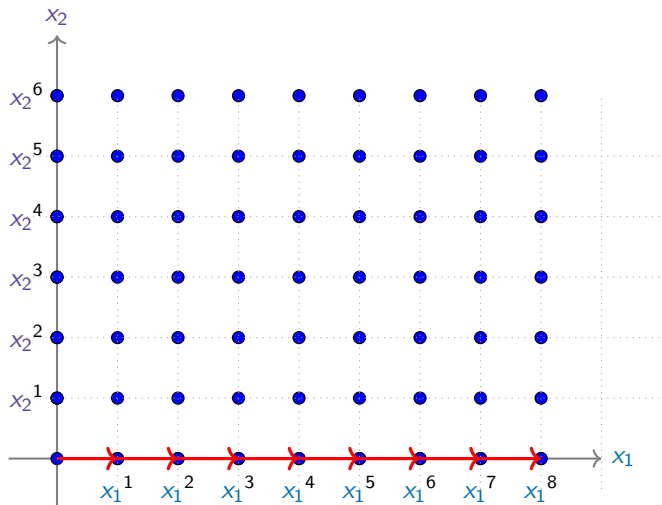
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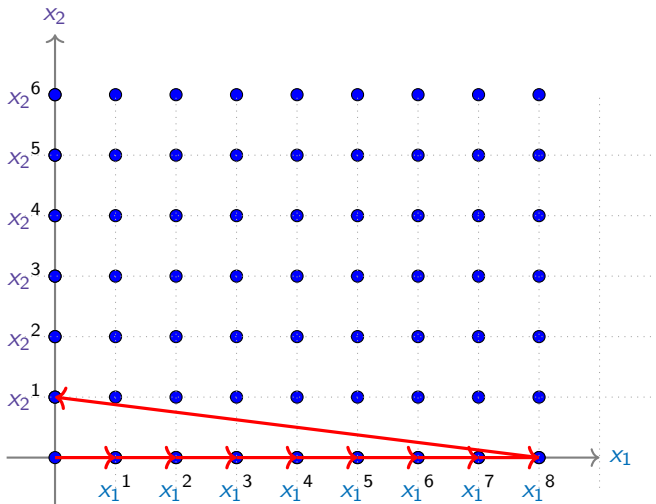
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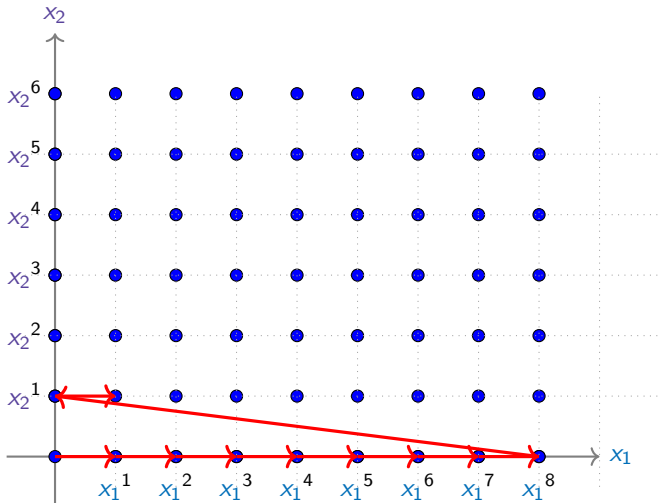
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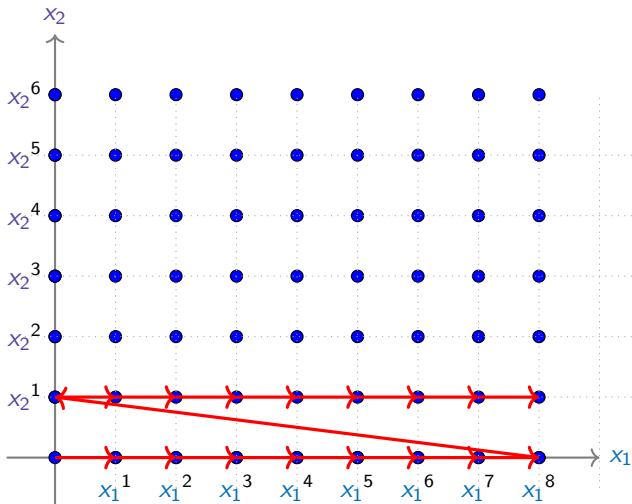
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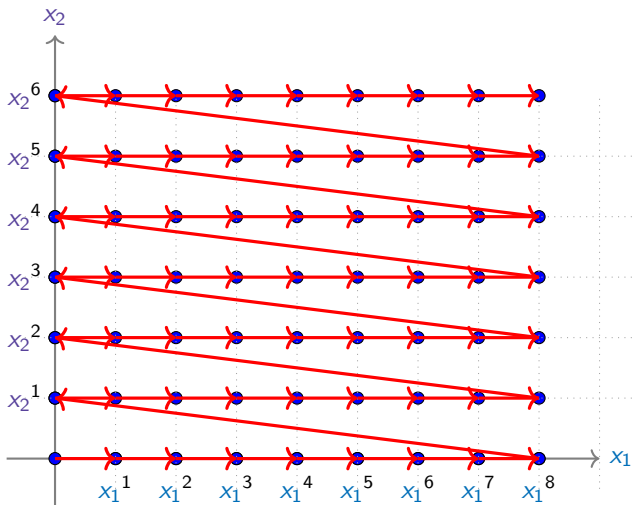
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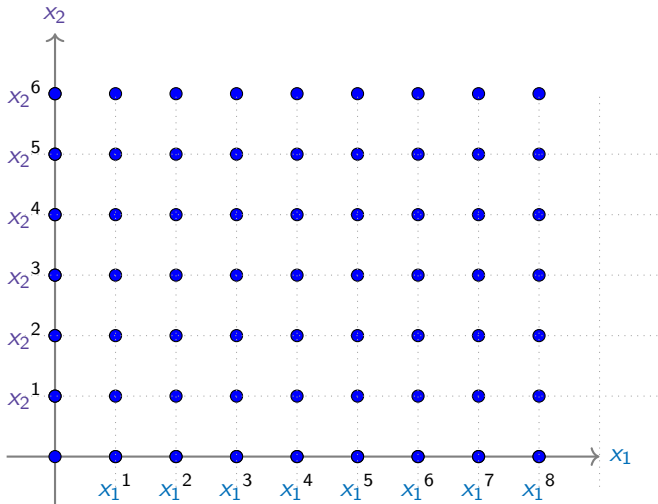
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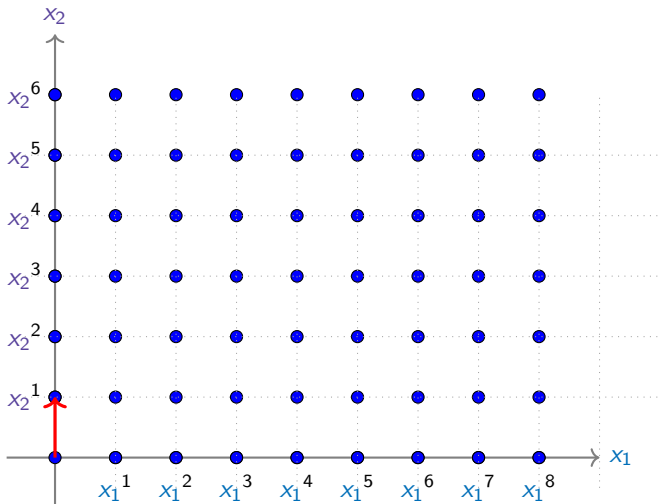
Reverse lex. ordering



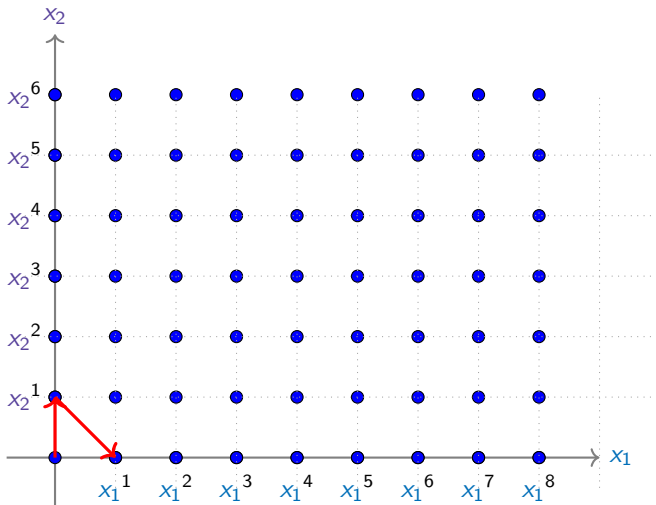
Graded lex. ordering



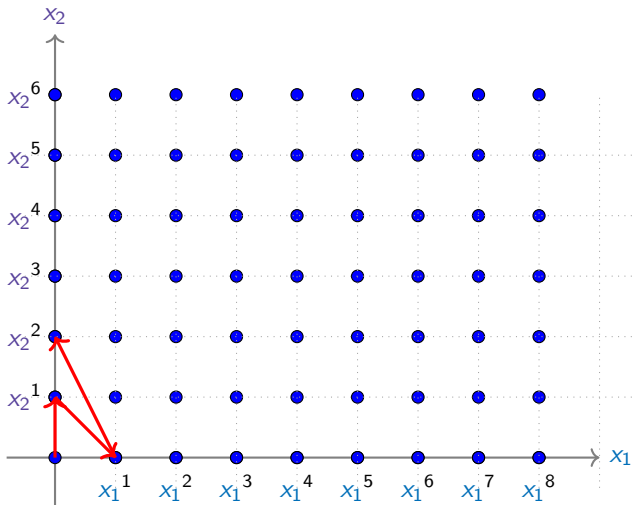
Graded lex. ordering



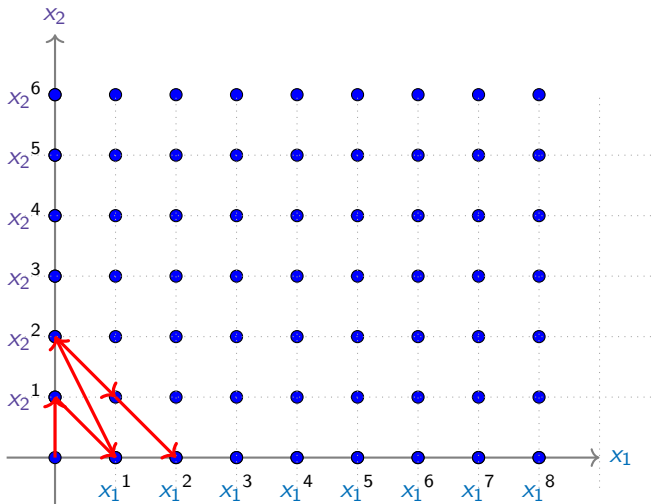
Graded lex. ordering



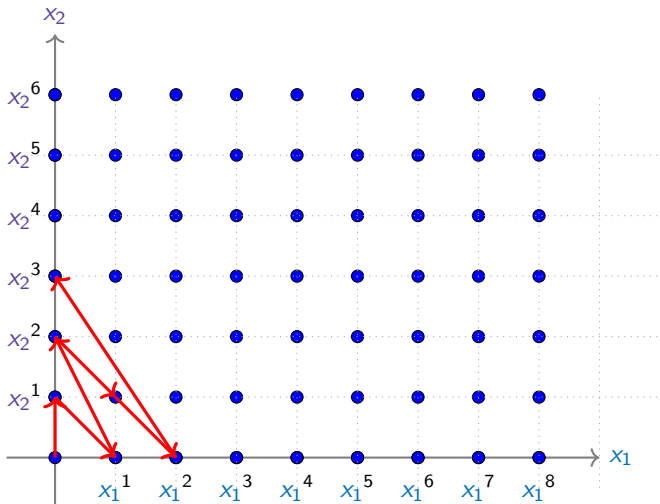
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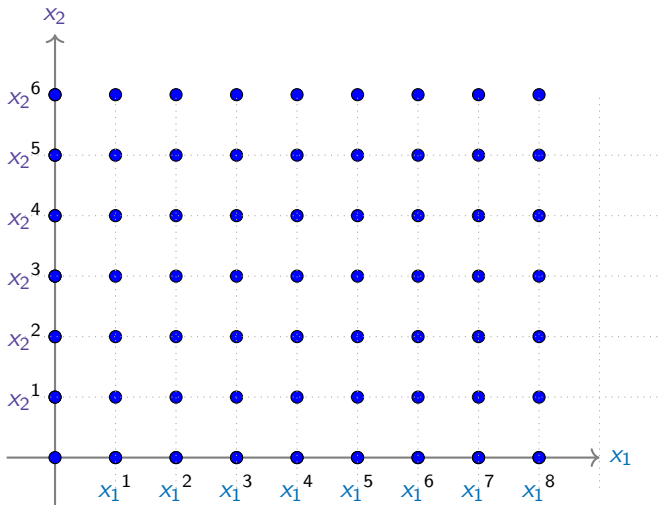
Graded lex. ordering



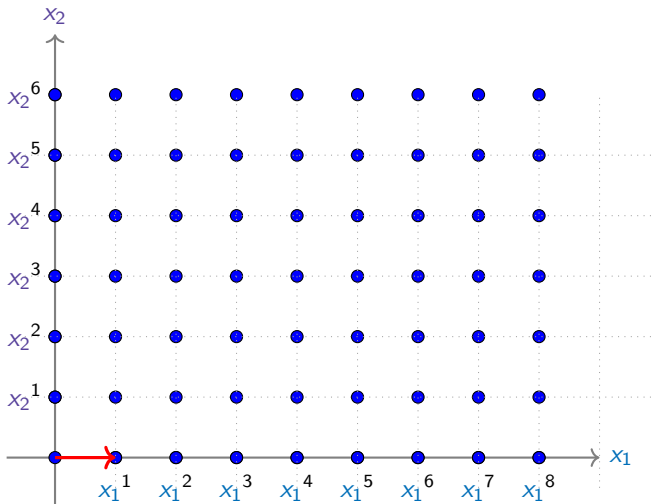
Graded lex. ordering



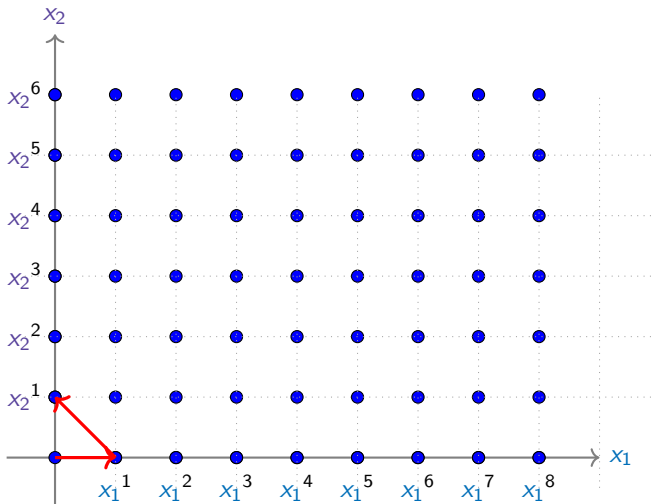
Graded reverse lex. ordering



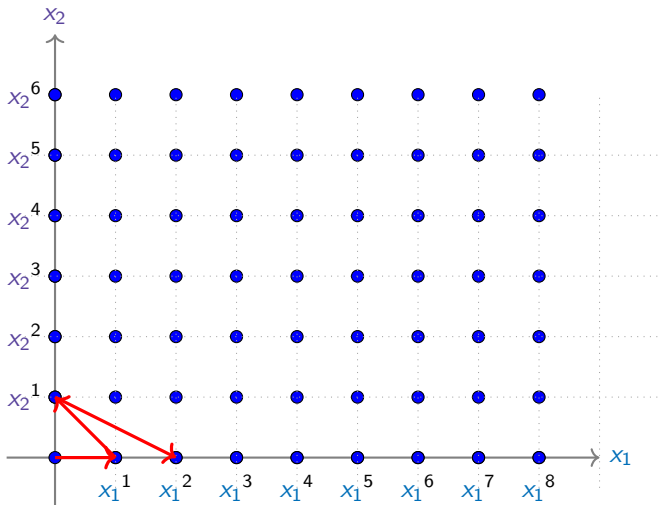
Graded reverse lex. ordering



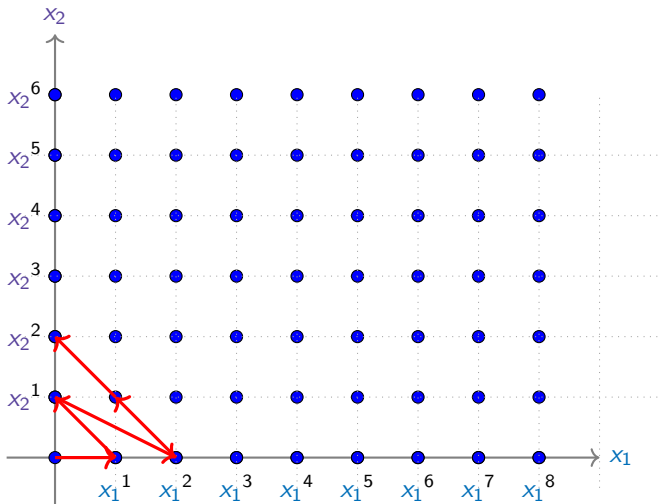
Graded reverse lex. ordering



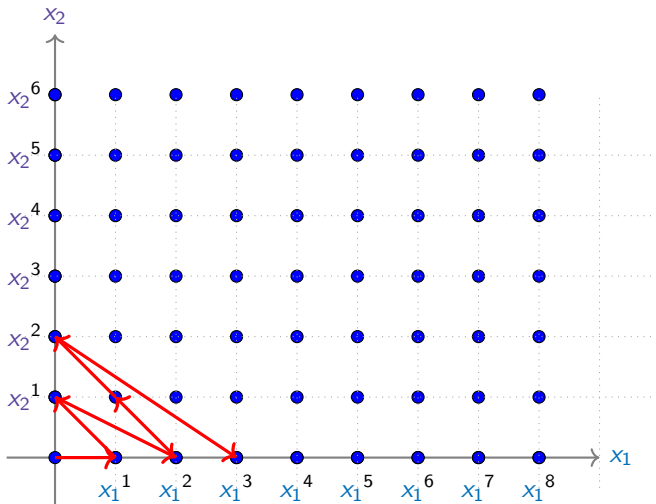
Graded reverse lex. ordering



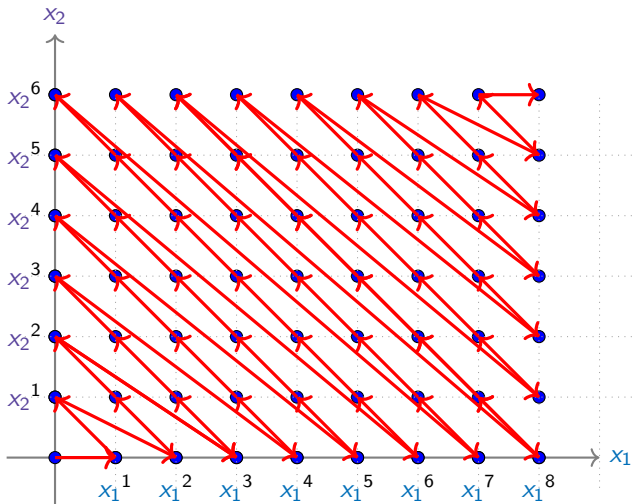
Graded reverse lex. ordering



Graded reverse lex. ordering



Graded reverse lex. ordering



Monomial ordering

Some orderings in $\mathbb{F}_q[x_1, x_2, x_3]$.

Lexicographical order (lex)

First, compare degrees of highest variable, then second variable, ...

$$x_1 > x_2 > x_3, \quad x_1 > x_2^2,$$

$$x_1^2 x_2 > x_1^2 x_3$$

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Graded lex. order (grlex)

First, compare total degree, then lex. order if equality.

$$x_1 > x_2 > x_3, \quad x_1 < x_2^2,$$
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Graded reverse lex. order (grevlex)

First, compare total degree, then inverse lex. order if equality.

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First, compare total degree, then inverse lex. order if equality.

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$$x_1^2 x_2 < x_1^2 x_3$$

Weighted graded lex. order

First, compare weighted sum of degrees, then graded lex. order.

If $\text{wt}(x_1) = 3$, $\text{wt}(x_2) = 1$ and $\text{wt}(x_3) = 4$, then

$$x_1 < x_2^2 x_3$$

Solving polynomial systems

★ **Univariate** solving: find the roots of $\mathcal{P}_j \in \mathbb{F}_q[X]$

$$\begin{cases} \mathcal{P}_0(X) & = 0 \\ & \vdots \\ \mathcal{P}_{m-1}(X) & = 0. \end{cases}$$

★ **Multivariate** solving: find the roots of $\mathcal{P}_j \in \mathbb{F}_q[X_0, \dots, X_{n-1}]$

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- ★ Compute a **grevlex order GB** (**F5** algorithm)
- ★ Convert it into **lex order GB** (**FGLM** algorithm)
- ★ Find the roots in \mathbb{F}_q^n of the GB polynomials using **univariate system resolution**.

Strategies

How to efficiency solve polynomial systems to build algebraic attacks?

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- ★ by **bypassing some rounds** of iterated constructions
- ★ by changing the **modeling**
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How to efficiency solve polynomial systems to build algebraic attacks?

- ★ by **bypassing some rounds** of iterated constructions
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- ★ by changing the **ordering**
- ★ by doing **nothing??**



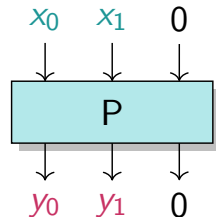
Ethereum Foundation Challenges

<https://www.zkhashbounties.info/>
(November 2021)



Solving CICO Problem

- ★ Feistel–MiMC [Albrecht et al., 2016]
- ★ POSEIDON [Grassi et al., 2021]
- ★ Rescue–Prime [Aly et al., 2020]
- ★ Reinforced Concrete [Grassi et al., 2022]



Ethereum Challenges: solving CICO problem for AO primitives with $q \sim 2^{64}$ prime

A. Bariant, C. Bouvier, G. Leurent, L. Perrin, 2022

Cryptanalysis Challenge

Category	Parameters	Security level	Bounty
Easy	$r = 6$	9	\$2,000
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Medium	$r = 14$	22	\$6,000
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(a) *Feistel–MiMC*

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(b) *Rescue–Prime*

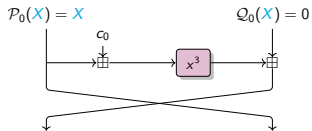
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(c) POSEIDON

Category	Parameters	Security level	Bounty
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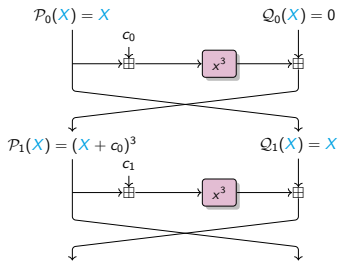
(d) *Reinforced Concrete*

Feistel-MiMC



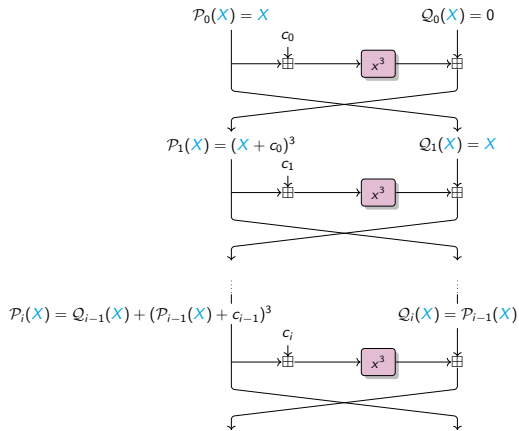
$$\left\{ \begin{array}{l} P_0(X) = X \\ Q_0(X) = 0 \end{array} \right.$$

Feistel-MiMC



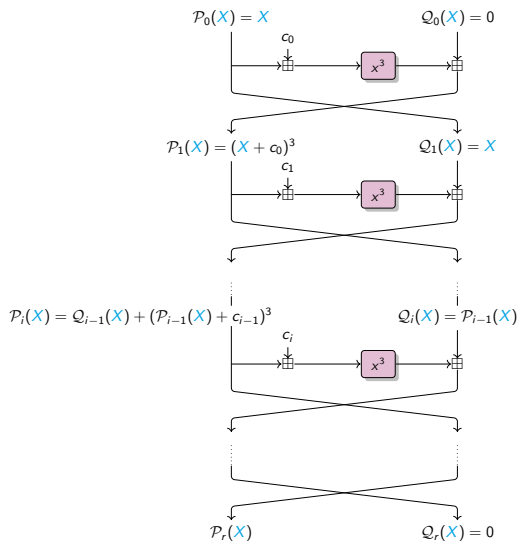
$$\left\{ \begin{array}{l} P_0(X) = X \\ Q_0(X) = 0 \\ P_1(X) = (X + c_0)^3 \\ Q_1(X) = X \end{array} \right.$$

Feistel-MiMC



$$\left\{ \begin{array}{l} \mathcal{P}_0(X) = X \\ \mathcal{Q}_0(X) = 0 \\ \mathcal{P}_1(X) = (X + c_0)^3 \\ \mathcal{Q}_1(X) = X \\ \dots \\ \mathcal{P}_i(X) = \mathcal{Q}_{i-1}(X) + (\mathcal{P}_{i-1}(X) + c_{i-1})^3 \\ \mathcal{Q}_i(X) = \mathcal{P}_{i-1}(X) \end{array} \right.$$

Feistel-MiMC



$$\left\{ \begin{array}{l} P_0(X) = X \\ Q_0(X) = 0 \\ P_1(X) = (X + c_0)^3 \\ Q_1(X) = X \\ \dots \\ P_i(X) = Q_{i-1}(X) + (P_{i-1}(X) + c_{i-1})^3 \\ Q_i(X) = P_{i-1}(X) \\ \dots \\ Q_r(X) = 0 \end{array} \right.$$

1 variable + $(2r + 1)$ equations

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(b) Rescue–Prime

\$12,000

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(c) POSEIDON

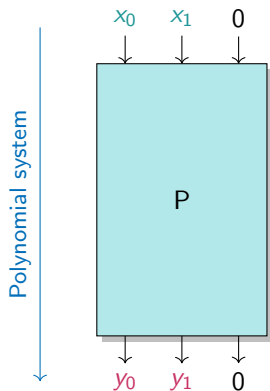
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(d) Reinforced Concrete

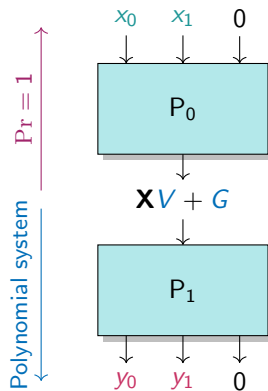
Trick for SPN

Let $P = P_0 \circ P_1$ be a permutation of \mathbb{F}_p^3 and suppose

$$\exists V, G \in \mathbb{F}_p^3, \quad \text{s.t.} \quad \forall \mathbf{X} \in \mathbb{F}_p^3, \quad P_0^{-1}(\mathbf{X}V + G) = (*, *, 0).$$

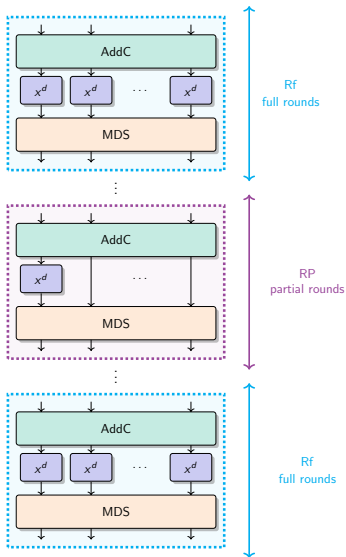


(a) R -round system.



(b) $(R - 2)$ -round system.

POSEIDON



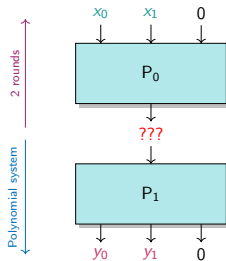
★ S-box:

$$x \mapsto x^3$$

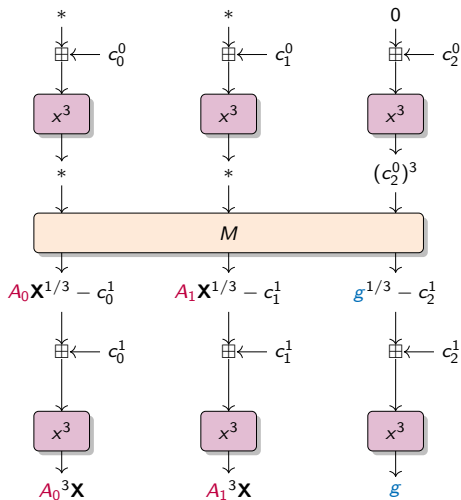
★ Nb rounds:

$$R = 2 \times Rf + Rp$$

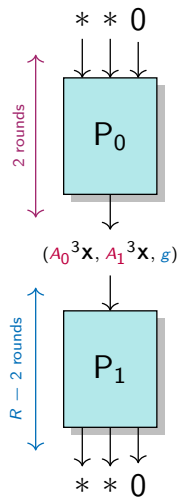
$$= 8 + (\text{from 3 to 24})$$



Trick for POSEIDON

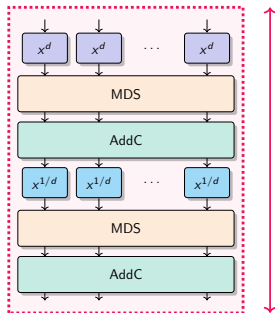


(a) First two rounds.



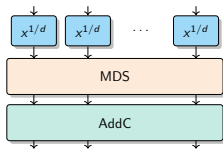
(b) Overview.

Rescue-Prime



1 round
(2 steps)

⋮



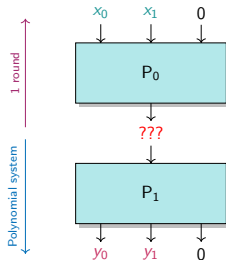
★ S-box:

$$x \mapsto x^3 \quad \text{and} \quad x \mapsto x^{1/3}$$

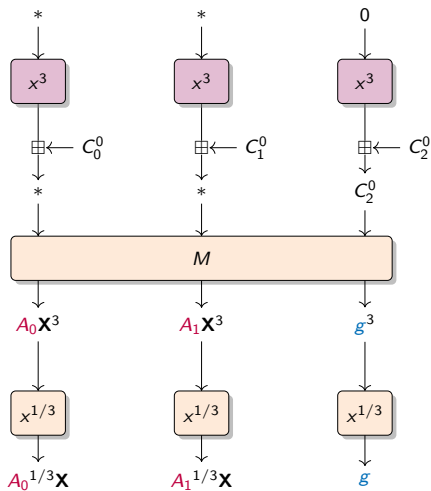
★ Nb rounds:

$R =$ from 4 to 8

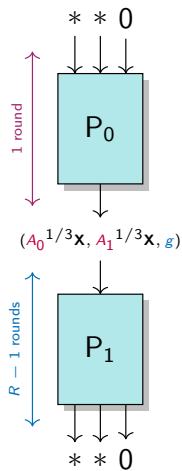
(2 S-boxes per round)



Trick for Rescue–Prime



(a) First round.



(b) Overview.

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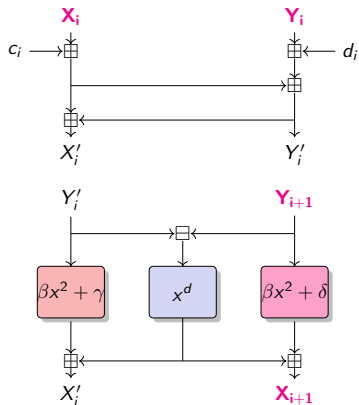
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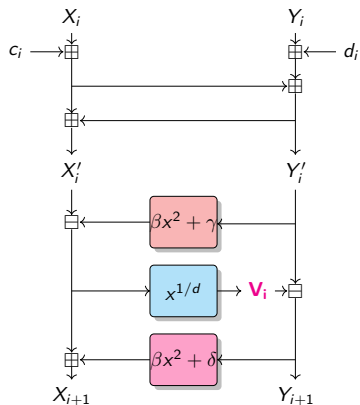
(d) Reinforced Concrete

Modeling of Anemoi

C. Bouvier, P. Briaud, P. Chaidos, L. Perrin, R. Salen, V. Velichkov and D. Willems, 2023

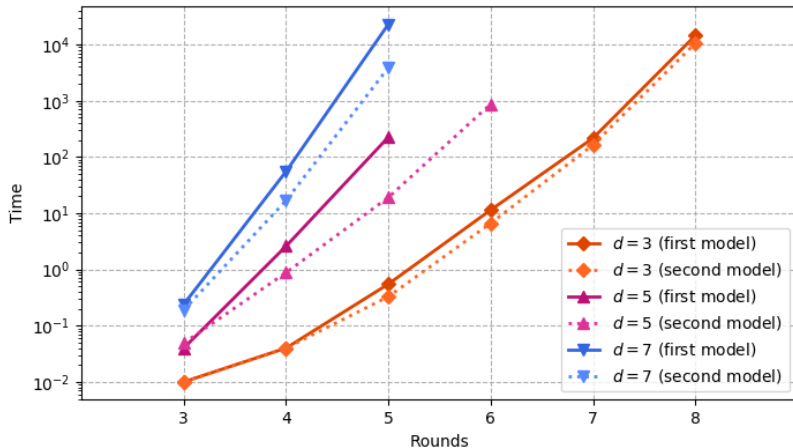


Model 1.



Model 2.

Importance of modeling



FreeLunch attack

A. Bariant, A. Boeuf, A. Lemoine, I. Manterola Ayala, M. Øygaard, L. Perrin, and H. Raddum, 2024

Multivariate solving:

- ★ Define the system
- ★ Compute a **grevlex order GB** (**F5** algorithm)
- ★ Convert it into **lex order GB** (**FGLM** algorithm)
- ★ Find the roots in \mathbb{F}_q^n of the GB polynomials using **univariate system resolution**.

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New Challenges

<https://www.poseidon-initiative.info/>
(November 2024)



New winners

More than \$30,000

A. Bak,
A. Bariant,
A. Boeuf,
M. Hostettler,
G. Jazeron

and others...

- Poseidon-256:
 - ~~24-bit estimated security: RF=6, RP=8. \$4000 claimed 9 Dec 2024~~
 - ~~28-bit estimated security: RF=6, RP=9. \$6000 claimed 2 Jan 2025~~
 - 32-bit estimated security: RF=6, RP=11. \$10000
 - 40-bit estimated security: RF=6, RP=16. \$15000
- Poseidon-64:
 - 24-bit estimated security: RF=6, RP=7 \$4000
 - 28-bit estimated security: RF=6, RP=8. \$6000
 - 32-bit estimated security: RF=6, RP=10. \$10000
 - 40-bit estimated security: RF=6, RP=13. \$15000
- Poseidon-31:
 - 24-bit estimated security: ~~RF=4, RP=0 (M31) claimed 29 Nov 2025~~ and ~~RP=1 (KoalaBear). \$4000 -claimed 30 Nov 2025~~
 - 28-bit estimated security: ~~RF=4, RP=1 (M31) and RP=3 (KoalaBear). \$6000 claimed 29 Nov 2025~~
 - 32-bit estimated security: ~~RF=6, RP=1 (M31) - claimed 2 Dec 2025~~ and ~~RP=4 (KoalaBear). \$10000 claimed 5 Dec 2025~~
 - 40-bit estimated security: RF=6, RP=4 (M31 only). \$15000

QUIZ !!

Could we use our trick for SPN on Reinforced Concrete?



QUIZ !!

Could we use the FreeLunch attack on Feistel–MiMC?



Conclusions and Perspectives

Conclusions

- ★ try as many modeling as possible
- ★ prefer univariate instead of multivariate system
- ★ be careful of tricks to bypass rounds

AOP: a new lucrative business?

Website

STAP Zoo

[STAP primitive types](#) [STAP use-cases](#) [All STAP primitives](#)

STAP

Symmetric Techniques for Advanced Protocols



The term STAP (Symmetric Techniques for Advanced Protocols) was first introduced in STAP'13, an affiliated workshop of Eurocrypt'13. It generally refers to algorithms in symmetric cryptography specifically designed to be efficient in new advanced cryptographic protocols. These contexts include zero-knowledge (ZK) proofs, secure multiparty computation (MPC) and (fully) homomorphic encryption (FHE) environments. It encompasses everything from arithmetization-oriented hash functions to homomorphic encryption-friendly stream ciphers.

STAP Zoo

We present a collection of proposed symmetric primitives fitting the STAP description and keep track of recent advances regarding their security and consequent updates. These may be filtered according to their features; we categorize them into different groups regarding primitive-type ([block cipher](#), [stream cipher](#), [hash function](#) or [PRF](#)) and use-case ([EHE](#), [MPC](#) and [ZK](#)).

For each STAP-primitive, we provide a brief overview of its main cryptographic characteristics, including:

- Basic general information: designers, year, conference/journal where it was first introduced and reference.
- Basic cryptographic properties such as description of the primitive (and relevant diagrams when applicable), use-case and proposed parameter sets.
- Relevant known attacks/weaknesses.
- Properties of its best hardware implementation.

When applicable, we also mention connections and relations between different designs.

See more at

stap-zoo.com



Website

STAP Zoo

STAP primitive types

STAP use-cases

All STAP primitives

STAP

Symmetric Techniques for Advanced Protocols



The term *STAP* (Symmetric Techniques for Advanced Protocols) was first introduced in *STAP'13*, an affiliated workshop of *Eurocrypt'13*. It generally refers to algorithms in symmetric cryptography specifically designed to be efficient in new advanced cryptographic protocols. These contexts include zero-knowledge (ZK) proofs, secure multiparty computation (MPC) and (fully) homomorphic encryption (FHE) environments. It encompasses everything from arithmetization-oriented hash functions to homomorphic encryption-friendly stream ciphers.

STAP Zoo

We present a collection of proposed symmetric primitives fitting the STAP description and keep track of recent advances regarding their security and consequent updates. These may be filtered according to their features; we categorize them into different groups regarding primitive-type (*block cipher*, *stream cipher*, *hash function* or *PRF*) and use-case (*EHE*, *MPC* and *ZK*).

For each STAP-primitive, we provide a brief overview of its main cryptographic characteristics, including:

- Basic general information: designers, year, conference/journal where it was first introduced and reference.
- Basic cryptographic properties such as description of the primitive (and relevant diagrams when applicable), use-case and proposed parameter sets.
- Relevant known attacks/weaknesses.
- Properties of its best hardware implementation.

When applicable, we also mention connections and relations between different designs.

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Thank you

